$\begin{array}{c} MA114 \; Summer \; 2018 \\ Worksheet \; 14-Power \; Series \; Part \; 2-7/05/18 \end{array}$

1. Using the fact that $\frac{-2}{3x^2+4x+1}=\frac{1}{1+x}-\frac{3}{1+3x}$, find a power series expression for $\frac{1}{3x^2+4x+1}$ around x=0.

2. Use the same idea as above to give a series expression for $\ln(1+2x)$ given that $\int \frac{2 dx}{1+2x} = \ln(1+2x)$. You will want to manipulate the fraction $\frac{2}{1+2x} = \frac{2}{1-(-2x)}$ as above.

3. Write $(1+x^2)^-2$ as a power series. Hint: Use term-by-term differentiation.